



SplitKey – A Threshold Cryptography Case Study

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Company introduction and background

- ⊙ R&D intensive ICT company in Estonia
 - ⊙ Research applied to practical security solutions since 1996
 - ⊙ Researched time stamping, PKI, digital signatures, multi-party computation, ...
 - ⊙ Developed and maintains Estonia's X-Road (UXP), i-voting, Sharemind, ...
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 - ⊙ About 140 employees, 15% of them with PhDs
- ⊙ Estonia/Latvia/Lithuania so far had three widely used methods of authentication
 - ⊙ ID-cards (smart-cards), Mobile-ID (SIM based), and one-time code cards
 - ⊙ 2014, EU PSD2 regulation came with **strong authentication** demand
 - ⊙ There was a market need for new kind of approach

SplitKey digital signature scheme

- ⊙ Software-based 2-out-of-2 threshold cryptosystem
- ⊙ Based on:
 - ⊙ Rivest, R., Shamir, A., Adleman, L.: A method for obtaining digital signatures and public-key cryptosystems. (1978)
 - ⊙ Desmedt, Y., Fraenkel, Y.: Threshold cryptosystems. (1990)
 - ⊙ Damgard, I., Mikkelsen, G. L., Skeltved, T.: On the security of distributed multiprime RSA. (2015)
 - ⊙ Camenisch, J., Lehmann, A., Neven, G., Samelin, K.: Virtual Smart Cards: How to sign with a password and a server. (2016)

SplitKey key pair generation and signing operation

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- ⊙ Composite signature: $s = CRT_{n_1, n_2}(s_1, s_2)$

Security reduction to the RSA

- ⊙ If RSA is S -secure against existential forgeries via adaptive chosen message attack, then the composite signature is about $\frac{S}{t_{ex}}$ -secure against the same attack, where t_{ex} is the time for one modular exponentiation

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Security strength (bits)	Symmetric key algorithms	RSA modulus n (bits)	SplitKey composite modulus $n_1 n_2$ (bits)
112	3TDEA	2048	6144
128	AES-128	3072	8192
192	AES-192	7680	16384

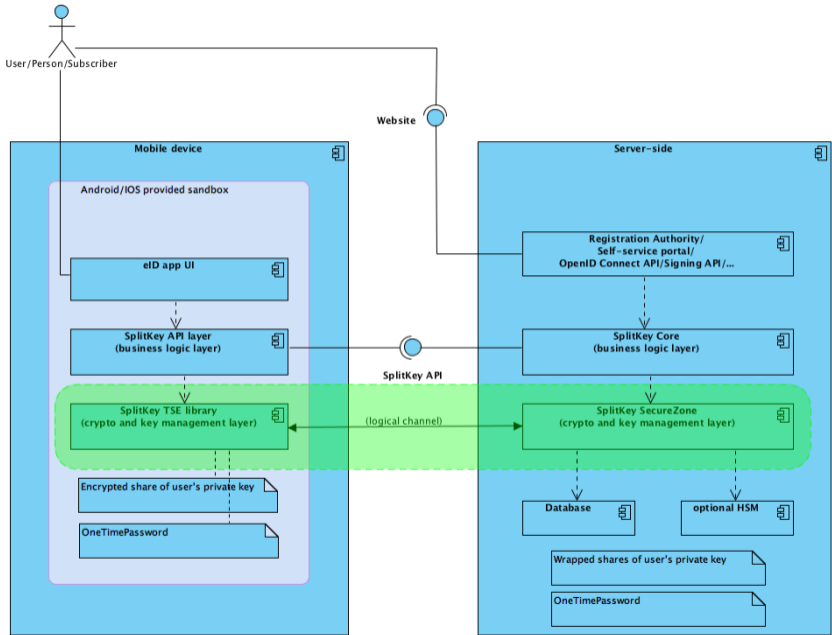
eIDAS QSCD/Common Criteria evaluation

- ⊙ Based on the eIDAS regulation.
- ⊙ Old Secure Signature Creation Device PP: prEN 14169-2:2012
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- ⊙ Evaluation lab: TÜViT in Germany
- ⊙ Consultant lab: CCLabs in Hungary
- ⊙ Evaluation process started in the beginning of 2017 and finished in the end of 2018
- ⊙ Evaluation assurance level for server-side component: EAL4 + AVA_VAN.5
- ⊙ Evaluation assurance level for client-side component: EAL2



Covered threats in eIDAS QSCD

- ⊙ Signer enrolment: Enrolment Forgery, Random Guessable, PubKey Forgery, MITM
- ⊙ Signing process: PIN Guessing, Authentication Forgery, Access Control ByPass, Replay, MITM, Cloning, Tampering
- ⊙ Cryptographic: Signature Forgery, Hash Forgery
- ⊙ Other: Unauthorized System Access, Audit Log Forgery

Reduced threats, because of applied TC

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Policy security requirements for eIDAS QSCD

- ⊙ Private key: Randomness, Confidentiality, Sole Control to Signer
- ⊙ Signing process: Hash Integrity
- ⊙ Cryptographic: Cryptographically Secure Signature Scheme
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Fulfilled requirements, because of applied TC

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Smart-ID – A commercial service with SplitKey

- ⊙ Legally compliant digital signature (eIDAS) and strong authentication service (PSD2) in Europe
- ⊙ Developed and operated by SK Identity Solutions AS, a private company in Estonia.



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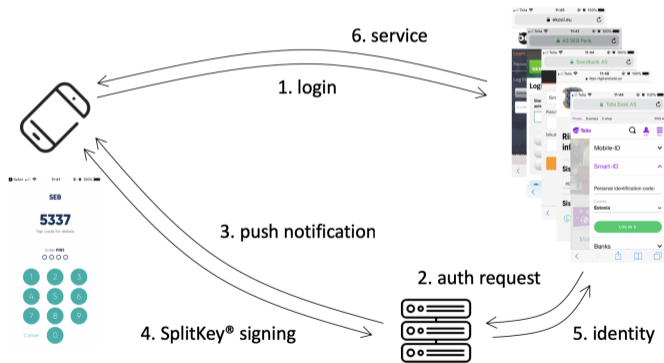
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- ⊙ SplitKey was originally developed for the Smart-ID service, now spun off to independent product line

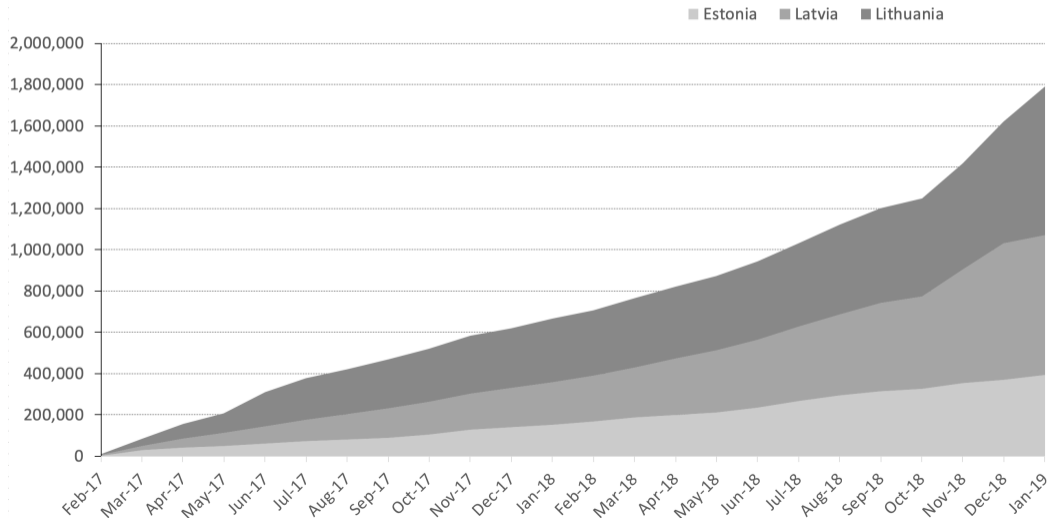


Smart-ID authentication flow

- ⦿ Authentication is started from the RP's webpage or RP's app, custom REST API.
- ⦿ OpenID Connect API supported, but not widely used.



Smart-ID uptake since the launch



Smart-ID uptake and usage

- ⊙ 1.88 M active users in total
- ⊙ 35% of adult population in Estonia, Latvia, and Lithuania
- ⊙ 43% - 49% of smartphone users
- ⊙ 30 M transactions per month

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Questions?